



## Notes – Introduction

- I. Introduction
  - a. Course Materials
    - i. Smith & Grant online. Nothing to buy
    - ii. Language: OCaml
    - iii. Emacs, or any text editor
    - iv. Homework submitted using Submit.
  - b. Coursework
    - i. Regular readings as a recommended lecture supplement
    - ii. Homework
      - 1. Weekly
      - 2. 50% of final grade
    - iii. Late policy: 10 points per day, up to 7 days
    - iv. Tests
      - 1. Other 50% of grade
      - 2. Midterm (20%)
      - 3. Final (30%)
    - v. Cheating: Conceptual collaboration okay, just don't copy anything.
  - c. Suggestions
    - i. The course is very systematic: concrete steps
    - ii. Don't miss anything.
    - iii. Tests are open-notes, so take good notes.
    - iv. Don't think of OCaml the same way as C++ or Java
- II. Overview
  - a. Central Concepts
    - i. Computability
      - 1. How to precisely characterize computing power
      - 2. Necessary features of programming languages to realize that power.
    - ii. Syntax (form), Semantics (meaning)
    - iii. Static Analysis (types)
      - 1. "Things you can tell by looking at code"
      - 2. Can get certain information about the program just by looking at the code statically.
    - iv. Reasoning about programs
  - b. Organization
    - i. First half: OCaml language
    - ii. Second half: Using OCaml to implement an interpreter for a small language
- III. Computability
  - a. "Computers" (electronic) are just one instance of the broader concept of "computing device."
  - b. Functions
    - i. Definition: A function, set theoretically, is defined as a set of ordered pairs  $(x, y)$  such that if there exists  $(a, b)$  in  $f$  and  $(a, b')$  in  $f$ , then  $b = b'$ .
    - ii. Example: Doubling Function =  $\{(1, 2), (2, 3), \dots\}$
    - iii. Definition: Given a function  $f$ , the domain of  $f$ , written  $\text{dom}(f)$  is  $\{x \mid (x, y) \in f\}$ . The range of  $f$ , written  $\text{rng}(f)$  is  $\{y \mid (x, y) \in f\}$ .
    - iv. Doesn't necessarily state that  $f(x)$  is computable!
  - c. Computability
    - i. Common notion: A procedure is computable on a given input iff it can be described in a finite manner as a set of definite actions and provides an output in a finite amount of time.
    - ii. Any formal definition devised so far conforms to this common notion.
    - iii. Note the time constraint. It needs only be finite. Efficiency is not addressed. Thus, an algorithm that takes billions of years is still considered computable.

- d. Turing Machines
  - i. Developed in 1930s by Alan Turing
  - ii. Idealized computing device, doesn't exist.
  - iii. A TM is comprised of...
    - 1. An indefinitely long tape (NOT infinite, just indefinitely long) divided into squares containing either 1 or 0.
    - 2. A read/write shift head (moves left and right) that can see one square at a time.
    - 3. An input card hopper capable of reading instructions from cards.
    - 4. A small region of internal memory containing an internal state ID (arbitrarily large integer)
  - iv. State IDs
    - 1.  $s_1, s_2, s_3, \dots$
    - 2. At any given moment, a Turing machine will be in a particular configuration
    - 3. Its configuration consists of the value currently under the reading head, together with the current state ID.
    - 4. Start configuration is  $(s_1, n_s)$  where  $n_s$  is the value under the reading head, given the initial tape.
  - v. Programming
    - 1. Input cards of the form  $\langle S_i, n, a, S_f \rangle$  (a quadruple)
      - a.  $S_i$  specifies the initial state.
      - b.  $n$  specifies the current read/write value
      - c.  $a$  specifies the definite action
        - i. Write 1
        - ii. Write 0
        - iii. Shift left
        - iv. Shift right
        - v. Halt
      - d.  $S_f$  specifies the result state.
    - 2. Cards are ordered, but are NOT "if..then" instructions in the traditional sense. Whichever card represents the current configuration gets executed.
    - 3. The reason the cards must be ordered is that two cards may contain the same  $S_i$  and  $n$ , in which case the first card is executed.
    - 4. Clearly very difficult for humans to program.
    - 5. "Computable" means that if the tape is initialized with  $x$ , then there exists a stack of cards such that the machine will halt with  $f(x)$  on the tape.
  - vi. Non-Termination
    - 1. Consider the card  $\langle s_1, 0, \text{Write } 0, s_1 \rangle$
    - 2. Assuming the tape starts with 0, the program never ends.
    - 3. Much more than just an annoyance to the programmer.
    - 4. Any Turing-Complete language will have this "feature."
    - 5. Fact (Halting Problem): There is no computable procedure for deciding whether an arbitrary TM will halt on a given input.

- IV. Programming Languages for Electronic Computers
  - a. Instruction set: Basic, primitive operations.
  - b. Machine Level languages specify procedures in terms of instruction sets.
  - c. Like card stacks for Turing Machines, very difficult and error prone for humans to use.
  - d. High Level Languages (HLLs) specify procedures at a much more abstract level: a level that's easy for humans to understand.
  - e. Even when using HLLs, we don't change the instruction set of the computer.
    - i. Need a translator of some kind.
    - ii. Compiled Languages

1. Most efficient implementation
2. Compilers are extremely complex.
  - a. Take HLL and translate into machine level.
  - b. Very complicated.
  - c. Most complex software in existence in terms of the amount of theory involved.
3. Interpreted Language
  - a. An interpreter of the language written in another HLL
  - b. Correctly implements constructs in terms of the other HLL
  - c. For example, an interpreter in C++ would determine the meaning of a statement and then execute it by running some C++ code.
4. NB: Any Turing-Complete language can interpret itself (called meta circularity)



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